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In the case of Graph Coloring, CP looks simple: after we've made a search step (instantiated a node with a color), propagate the color at that node.

PropagateColorAtNode(node,color)

- 1. remove color from all of "available lists" of our uninstantiated neighbors.
- 2. If any of these neighbors gets the empty set, it's time to backtrack.
- Foreach n in these neighbors: if n previously had two or more available colors but now has only one color c, run PropagateColorAtNode(n,c)

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Job-shop: the Variables and Constraints

Variables

- The operation state times stⁱ_i
- The resources Rⁱ_{ij} (usually these are obvious from the definition of Oⁱ_i. Only need to be assigned values when there are alternative physical resources available, e.g. *Pat* or *Chris* for operating the *drill*).

Constraints:

- Precedence constraints. (Some O's must be before some other O's).
- Capacity constraints. There must never be a pair of operations with overlapping periods of operation that use the same resources.

Non-challenging question. Can you schedule our Job-shop?

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Job-shop example. Consistency enforcement

Sadeh claims that generally forward-checking is better, computationally, than full constraint propagation. But it can be supplemented with a Job-shop specific TRICK.

The precedence constraints (i.e. the available times for the operations to start due to the ordering of operations) can be computed exactly, given a partial schedule, very efficiently.

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Reactive CSP solutions

- Say you have built a large schedule.
- Disaster! Halfway through execution, one of the resources breaks down. We have to reschedule!
- Bad to have to wait 15 minutes for the scheduler to make a new suggestion.

Important area of research: efficient schedule repair algorithms.

- Question: If you expect that resources may sometimes break, what could a scheduling program do to take that into account?
- Unrelated Question: Why has none of this lecture used A*?
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Other approaches. And What You Should Know

Other Approaches:

 Hill-climbing, Tabu-search, Simulated annealing, Genetic Algorithms. (to be discussed later)

What you should know:

- ✓ How to formalize problems as CSPs
- ✓ Backtracking Search, Forward Checking, Constraint Propagation
- ✓ The Waltz algorithm
- ✓ You should understand and appreciate the way job-shop scheduling is formalized. It is an excellent representative example of how important well-studied constraint satisfaction problems are represented.
- Understand examples of Variable ordering and Value ordering heuristics

In those cases where your lecturer or these handouts are too incomprehensible, consult Chap 5 of the Russell handout. Winston's "Artificial Intelligence" book has good discussion of constraint satisfaction and Waltz algorithm.

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